FeaStNet: Feature-Steered Graph Convolutions for 3D Shape Analysis

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Computer Vision and Pattern Recognition, 2018

ConvNets are everywhere for 2D images





Detection





Retrieval Segmentation [Krizhevsky et al., 2012, Farabet et al., 2013, Ren et al., 2015, Gordo et al., 2016]

Convolutional Neural Networks (CNNs)



[LeCun et al., 1989]

How to generalize ConvNets to graph-structured data?

- RGB over regular grid of pixels
- ► XYZ(+RGB) over irregular graph of vertices



Applications





knowledge graphs



molecular graphs



social network analysis

Problem: Shape correspondence



Problem: Shape correspondence



Representations for 3D shape data



Extrinsic vs. Intrinsic representations



Figure from [Boscaini et al., 2016]

Extrinsic representation: Voxel grids

- Occupancy grids on input and/or output
- Quantize space rather than shape, lots of empty space
- 3D convolutions over grid, limited scalability
 - Sparse convolutions over input [Graham et al., 2018]
 - Octtrees on input and/or output [Tatarchenko et al., 2017]



Extrinsic representation: Point clouds

- Avoid quantization, ignore (most) structure
- PointNet [Qi et al., 2017]
 - ► Local per-point processing (1×1 convolution)
 - Global max-pooling for global shape properties

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 - Global max-pooling for global shape properties
- Kd-Networks [Klokov and Lempitsky, 2017]
 - Propagate features across Kd-Tree over point cloud
 - Share parameters over branches with same split direction



 Local geodesic polar coordinates [Masci et al., 2015, Boscaini et al., 2016]

$$\mathbf{u}(x,y) = (\rho(x,y), \theta(x,y))$$



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- Trained filters, hand-crafted patch function



MoNet: Trainable patch function [Monti et al., 2017]

▶ Trainable Gaussian assignment to bin *k* of the patch

$$\mathbf{u}(x,y) = (\rho(x,y), \theta(x,y)) \tag{1}$$

$$w_k(\mathbf{u}) = \exp((\mathbf{u} - \mu_k)^T \Sigma_k^{-1} (\mathbf{u} - \mu_k))$$
(2)

 Trained filters, trained patch function, hand-crafted features for patch function



Polar coordinates ρ, θ

FeaStNet: Feature-Steered Graph Convolutions

Generic graph-convolutional network architecture

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- Generic graph-convolutional network architecture
- No hand-crafted features to design graph-convolution
- Validation: 3D shape correspondence and part labeling



Template

Texture transfer on test shapes











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$$y_i = b + rac{1}{|\mathcal{N}_i|} \sum_{m=1}^M W_m \sum_{j \in \mathcal{N}_i} q_m^{ij} x_j$$


Graph convolutional approach in FeaStNet

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Using ring-1 neighbors in practice, but can be different



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- Can use arbitrary subnet, simplest case: 1-layer + softmax

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▶ Setting u_m = −v_m in makes assignment translation invariant in feature space

$$q_m^{ij} \propto \exp\left(u_m^ op(x_j - x_i) + c_m
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 - Computational cost increased from O(NMED) to O(NME(D + K))

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- Can be implemented by translation invariant linear-softmax assignment function



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 - ► SHOT: Signature of Histograms of Orientations [Tombari et al., 2010]
 - XYZ: raw vertex coordinates



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 - ► SHOT: Signature of Histograms of Orientations [Tombari et al., 2010]
 - XYZ: raw vertex coordinates
- Correspondence as dense labeling problem
 - Like semantic segmentation, but with 6,890 classes



Shape correspondence: Architectures

- Single-scale architecture
 - $\blacktriangleright \ Lin16 + Conv32 + Conv64 + Conv128 + Lin256 + Lin6890$

Shape correspondence: Architectures

- Single-scale architecture
 - Lin16 + Conv32 + Conv64 + Conv128 + Lin256 + Lin6890
- Multi-scale architecture
 - Graph sub-sampling [Dhillon et al., 2007]
 - Max pooling, zero-pad up-sampling



Results single-scale architecture

Metric: Percentage of correct (exact) correspondences

Transinv.	yes	no
XYZ	86%	28%
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- Impact nr. of weight matrices, using XYZ



Geodesic errors: SHOT vs. XYZ

- Geodesic distance between predicted and true correspondence
- Single-scale architecture in both cases



► Metric: Percentage of correct (exact) correspondences

Method	Input	Accuracy
Logistic Regr., w/o refinement	SHOT	39.9%
GCNN [Masci et al., 2015], w/o refinement	SHOT	42.3%
PointNet [Qi et al., 2017], w/o refinement	SHOT	49.7%
ACNN [Boscaini et al., 2016], w/ refinement	SHOT	62.4%
GCNN [Masci et al., 2015], w/ refinement	SHOT	65.4%
MoNet [Monti et al., 2017], w/o refinement	SHOT	73.8%
MoNet [Monti et al., 2017], w/ refinement	SHOT	88.2%
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- New state of the art result, with both XYZ and SHOT
- ▶ Relative reduction of 89% in error rate w.r.t. Monti *et al.*

Geodesic errors

- Metric: Percentage of correspondences within tolerance
- Dashed curves: without refinement



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Without refinement: very few, relatively big errors

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- Without refinement: very few, relatively big errors
- With refinement: very few, very small errors










Shape correspondence: Noise robustness

 Gaussian noise on vertex coordinates, proportional to average distance to neighbors



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Shape correspondence: Noise robustness

- Gaussian noise on vertex coordinates, proportional to average distance to neighbors
- Robust model when training with noisy shapes



Feature activations

- Left: 4 features on same shape
- Right: same feature on 4 shapes



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- Single-scale architecture, with global max-pooling
- Descriptors: XYZ coordinates



Part labeling: Quantitative results

Performance similar to methods designed for point-cloud data

	overall	aero	car	chair	guitar	knife	lamp	laptop	motor	pistol	table
		plane							bike		
Number of shapes	16,881	2690	898	3758	787	392	1547	451	202	283	5271
PointNet [Qi et al., 2017]	83.7	83.4	74.9	89.6	91.5	85.9	80.8	95.3	65.2	81.2	80.6
KdNet [Klokov and Lempitsky, 2017]	82.3	80.1	70.3	88.6	90.2	87.2	81.0	94.9	57.4	78.1	80.3
FeaStNet	81.5	79.3	71.7	87.5	90.0	80.1	78.7	94.7	62.4	78.3	79.6

Part labeling examples

 Test shapes with accurate labeling, and one with worst labeling in category.



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- State-of-the-art 3D shape correspondence from raw XYZ
- Comparable to previous work on point cloud labeling
- Perspectives
 - Application to raw/real scanned 3D meshes
 - Integrate global correspondence refinement
 - Generalize across meshes/templates: local correspondences
 - Modeling meshes in motion: (shape + pose) x time

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